## Planning and Scheduling of Semi-Urgent Surgeries



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## Background

- Surgical department
- Three surgery types:
$\rightarrow$ Elective (planned in advance)
$\rightarrow$ Urgent (within 24 hours)
$\rightarrow$ Semi-urgent (within 1 or 2 weeks)
- Consider regularly scheduled hours


## Motivation

- (Semi-)Urgent surgeries pose uncertain demand on resources
- Urgent surgeries usually performed in overtime or at separate OR
$\rightarrow$ Not taken into account
- Semi-urgent surgeries may not be performed in overtime $\rightarrow$ Allocate part of regular OR hours to these surgeries


Very little: many elective patients canceled

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## Contents of this Talk

- Determine optimal amount of OR time to allocate to semi-urgent surgeries
$\rightarrow$ Queuing model
- Determine when semi-urgent surgeries should be scheduled $\rightarrow$ Markov decision model


## Case Study - Introduction

- Case to illustrate working of models
- Actual data obtained at Leiden University Medical Center
- Neurosurgery department
- 8 OR sessions per week
- $40 \%$ of all incoming surgeries is classified semi-urgent


## Queuing Model

- Determine optimal amount of OR time to allocate to semi-urgent surgeries
- Each semi-urgent surgery has estimated duration 1,2,..,K slots
- Model semi-urgent slot arrivals as a compound Poisson process
- Each OR session has duration K slots
- Total number of slots available (M) = \# OR sessions * K


## Queuing Model

- Total number of slots available (M) = \# OR sessions * K
- Allocate fraction (S) of M to semi-urgent slots
- Slotted queuing model in discrete time


## Queuing Model

- Note that
$\rightarrow$ \# of canceled elective slots $\left(N_{C}\right)$ depends on $S$
$\rightarrow$ \# of empty OR slots ( $\mathrm{N}_{\mathrm{E}}$ ) depends on S



## Queuing Model

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## Queuing Model

- Use queuing model to determine $\mathrm{E}\left[\mathrm{N}_{\mathrm{C}}\right]$ and $\mathrm{E}\left[\mathrm{N}_{\mathrm{E}}\right]$ for each S
- Assign cost $\mathrm{C}_{\mathrm{C}}$ to canceled elective slot
- Assign cost $\mathrm{C}_{\mathrm{E}}$ to empty OR slot
- Find $S^{*}$ that miminizes expected total cost:

$$
\mathrm{E}\left[\mathrm{C}_{\mathrm{T}}\right]=\mathrm{E}\left[\mathrm{~N}_{\mathrm{C}}\right]^{*} \mathrm{C}_{\mathrm{C}}+\mathrm{E}\left[\mathrm{~N}_{\mathrm{E}}\right] \mathrm{C}_{\mathrm{E}}
$$

- $S^{*}$ is the optimal number of slots to allocate to semi-urgent surgeries, given $C_{C}$ and $C_{E}$


## Case Study - Queuing Model

- Apply model to case study of neurosurgery department
- Total number of slots available (M) = 8*3 = 24
- On average 5.5 semi-urgent surgeries arrive per week
- $\mathrm{P}(1$ slot surgery) $=0.53$
- $\mathrm{P}(2$ slot surgery) $=0.20$
- $P(3$ slot surgery $)=0.27$
- $\mathrm{S}_{\text {min }}=$ expected number of semi-urgent slot arrivals $=9.6$ $\rightarrow$ Allocate at least 10 slots to obtain a stable system


## Case Study - Queuing Model



## Case Study - Queuing Model

- Optimal value of $S^{*}$ depends on choice of $\mathrm{C}_{\mathrm{C}}$ and $\mathrm{C}_{\mathrm{E}}$
- If $\left(C_{C}, C_{E}\right)=(1,1)$

$$
\rightarrow \mathrm{S}^{*}=13\left(\mathrm{E}\left[\mathrm{C}_{\mathrm{T}}\right]=4.77\right)
$$

- If $\left(C_{C}, C_{E}\right)=(1,10)$

$$
\rightarrow S^{*}=11\left(E\left[C_{T}\right]=19.42\right)
$$

- If $\left(C_{C}, C_{E}\right)=(10,1)$ $\rightarrow S^{*}=17(E[C T]=9.45)$
- Note that $\mathrm{S}^{*}>\mathrm{S}_{\text {min }}$ in all cases!


## Markov Decision Model

- Two types of semi-urgent surgeries:
$\rightarrow$ Surgery within one week
$\rightarrow$ Surgery within two weeks
- Schedule one-week semi-urgent surgeries this week
- Two-week semi-urgent surgeries can be postponed one week
- When to schedule two-week semi-urgent surgeries?


## Markov Decision Model

- Continue with slotted approach
- Schedule up to S*?



## Markov Decision Model

- Or more?
- Drawback: canceling of elective slots



## Markov Decision Model

- Then just up to S*? $^{*}$
- Risk of postponement: one-week semi-urgent surgeries performed in overtime

2 week slots from last week -


## Markov Decision Model

- Develop Markov Decision Model
- Determine for each state (combination of number of one- and two-week semi-urgent slots waiting) an action (how many two-week slots to plan this week)
- Use costs and related $\mathrm{S}^{*}$ calculated in queuing model
- Introduce additional costs for overflow of semi-urgent slots
- Minimize expected total discounted costs


## Case Study - Markov Decision Model

- Trivial problem?
- More than 1000 states for neurosurgery case study!
- Consider $\left(C_{C}, C_{E}\right)=(1,1) ;(1,10) ;(10,1)$
- Graphic representation of strategies


## Case Study - Markov Decision Model



## Case Study - Markov Decision Model



## Case Study - Markov Decision Model



## Conclusion

- Determine with queuing model how much OR time should be allocated to semi-urgent surgeries
$\rightarrow$ Optimal solution depends highly on costs
$\rightarrow$ Dangerous to focus only on average behavior
- Use Markov decision model to decide upon actual scheduling
$\rightarrow$ Simplifies scheduling job


## Questions?

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