The After Salesman Problem

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## From sales to after sales

Binnen 48 uur uw eigen installatiemonteur aan huis

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Uw PC krijgt een complete installatie en configuratie en geeft u waar nodig nog enkele instructies en tips. Ook softwarematige configuratie van internet behoort tot het pakket. Hierna kunt u direct zelf aan de slag! Dit alles in nog geen uurtje van uw tijd!

We are living in a service economy: (2007: +/- 74 \%)

## After sales = service

5 dimensions of service

- Tangibles
- Empathy
- Assurance
- Reliability
- Responsiveness
(Parasuraman 1985)


Erasmus MC

## More responsiveness

" Johnston (1995): Responsiveness influences customer satisfaction and dissatisfaction.

- Davis \& Heineke (1998) Actual waiting time is a key driver of customer satisfaction
- (Collier \& Wilson 19970, Brady \& Cronin 2001).....
- Footnote: perception of responsiveness determines satisfaction


## How to measure responsiveness?



## By average waiting time?

1. Go to John, service, John, go to Anita service Anita
Waiting time John : 60+30= 90

Waiting time Anita : $10+30+20+30=\quad 90$
Average waiting time: 90
2. Go to Anita, service Anita, go to John service John

Waiting time Anita:

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10+5=
$$

Waiting time John: $60+5+20+30=$
Average waiting time: 65

## 25 minutes later (how to measure responsiveness)



## By average waiting time?

1. Go to John, service, John, go to Cindy service Cindy
Waiting time John:
85+30= 115
Waiting time Cindy: $10+30+20+30=\quad 90$
Average waiting time:
102.5
2. Go to Cindy, service Cindy, go to John service John

Waiting time Cindy:
$10+5=$ 15
Waiting time John: $85+5+20+30=$
Average waiting time: 77.5

## performance indicators/ objectives

Unfit:

- Travel distance
- Idle time
- Travel cost
- Fuel usage
- Average waiting time
- Maximum waiting time
- Number of late services.....

Fit: Service Level Agreement on:

Waiting time treshhold per service request

- Time til repair treshhold per request
- Treshhold on total time out of service per month
- ......


## Related literature

- Queuing Models (Bertsimas \& Van Ryzin (1991), Irani et al. (2001)
- Focusses on theoretic properties
- Different objectives
" Dynamic pick up and delivery models (Gendreau et al. 1998, Ichoua et al. 2006)
- Many based on local search
- Focus on transportation applications, different objectives
- Work in road side service industry
- Practical work (AA, ADAC, ANWB,....)
- Krumke et al. (ZIBB) (2001 onwards)



## Background for remainder of work



## Sketch for remainder of presentation

- Introduction of 3 models
- Solution methods for the 3 models
- Discussion of problem characteristics and assumptions, through solution of models:
- Basic model
- Reoptimization frequency
- On line objectives versus end of day responsiveness
- Diversion
- Value of service time information
- Conclusions


## Modelling concept

The service problem reveals itself in real time:

Every $t$ time units ( 30 seconds),
See whether new requests or service man have arrived
See whether current services are being complete
Make new dispatch decisions if possible

The real time problem instances will be modelled and solved using a real time objective function

Thus, we gradually obtain a solution for the problem stretching over the entire planning period (day), and an end-of-day solution, measured by an end of day objective function.


## 3 real time models - I : FCFS

Repeatedly consider requests in order of arrival and assign the service man which maximizes the selected objective function

- 'fair' : customers will be serviced in order of arrival.


Solution: sorting (polynomial)

## 3 real time models - II: Matching



Find an optimal matching in the bipartite graph below


Solution: Hungarian algorithm $O\left(N^{3}\right)$

## 3 real time models - III: Set partitioning



Partition the set of all customers into tours such that the selected objective is optimized

## Solution of the Set Partitioning Model (Krumke et al. )

1. Solve LP relaxation (which has exponentially many columns) using column generation
2. Proceed using branch \& bound

- Not guaranteed to be optimal, but computational experiments show that solutions are very close to optimal.

Each of the dispatch models can be solved 'to optimality'. Hence we can compare the models, not the algorithms


## Simulation setting (modelled after practice)

- Poisson arrival process, interarrival time average varies from 100 (heavy) to 1000 seconds (light) .
- Exponentially distributed service times, average 15 minutes.
- Unformly distributed service request locations in R2.
- Domain of $125 \times 125 \mathrm{~km}$,
- 20 service men
- Average travel speed $=60 \mathrm{~km} / \mathrm{h}$.
- SLA treshhold: 60 minutes


## Basic computational results



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## Waiting time distribution



36 incidents per hour


## Reoptimization Frequency



## End of day objectives through real time objectives



SLA (+ waiting time) real time
compared to average waiting time

## End of day objectives through real time objectives



SLA (+ travel time)
compared to average waiting time

## End of day objectives through real time objectives



Average waiting time + average travel time compared to average waiting time


## Lesson learned so far

- FCFS is fair but not beneficial (on the contrary for heavy traffic scenarios)
- Matching is comparable to Set Partitioning, but the latter is significantly better under heavy traffic scenarios (the more competitive scenarios).
- Reoptimization frequency matters, it is better to reoptimize frequently under light traffic, and less frequently under heavy traffic
- Handle objectives with care: relation between real time and end of day performance is non obvious.


## Diversion helps!

$\square \quad \square, 6$
$\square 7,2$
$\square 10,8$
$\square 14,4$
$\square 18,0$
$\square 21,6$
$\square 25,2$
$\square 28,8$
$\square 32,4$
$\square 36,0$

Note: Only allowed when more than 7.5 minutes travel remaining
Note: Total end of day travel distance reduced as well

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## Perfect information on service duration



## Median duration instead of expected duration



## Lessons learned

- Median works better than average duration
- Knowing service durations perfectly is valuable
- More valuable is allowing for diversion (to use the real time visibility of the business process).

The difficulty appears to be in the stochastics of the arrival process rather than in the stochastics of the service processes.

## Knowing events in advance



## Conclusions

Practice: Use of ICT + OR can tremendously advance customer responsiveness

Practice: Optimization requires more than intuition and common sense

Theory: Theoretically largely unexplored area, many questions open

Theory: Deal with arrival stochastics (Larsen et al. 22004, Hvattum et al. 2006,2007, Van de Klundert \& Otten 2007) - e.g. via scenario based methods

Theory: Work on problems where locations of customers are oivent

## Questions?



